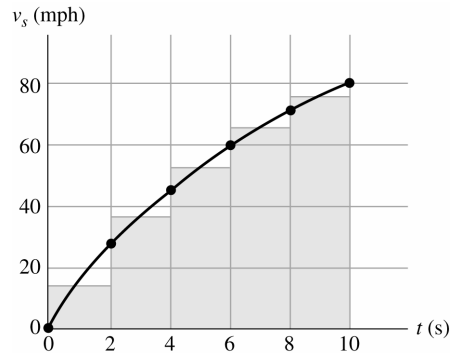


2.42. Model: The automobile is a particle.

Solve: (a)



The acceleration is not constant because the velocity-versus-time graph is not a straight line.

(b) Acceleration is the slope of the velocity graph. You can use a straightedge to estimate the slope of the graph at $t = 2$ s and at $t = 8$ s. Alternatively, we can estimate the slope using the two data points on either side of 2 s and 8 s. Either way, you need the conversion factor $1 \text{ mph} = 0.447 \text{ m/s}$ from Table 1.4.

$$a_x(\text{at } 2 \text{ s}) \approx \frac{v_x(\text{at } 4 \text{ s}) - v_x(\text{at } 0 \text{ s})}{4 \text{ s} - 0 \text{ s}} = 11.5 \frac{\text{mph}}{\text{s}} \times \frac{0.447 \text{ m/s}}{1 \text{ mph}} = 5.1 \text{ m/s}^2$$

$$a_x(\text{at } 8 \text{ s}) \approx \frac{v_x(\text{at } 10 \text{ s}) - v_x(\text{at } 6 \text{ s})}{10 \text{ s} - 6 \text{ s}} = 4.5 \frac{\text{mph}}{\text{s}} \times \frac{0.447 \text{ m/s}}{1 \text{ mph}} = 2.0 \text{ m/s}^2$$

(c) The displacement, or distance traveled, is

$$\Delta x = x(\text{at } 10 \text{ s}) - x(\text{at } 0 \text{ s}) = \int_0^{10 \text{ s}} v_x dx = \text{area under the velocity curve from } 0 \text{ s to } 10 \text{ s}$$

We can approximate the area under the curve as the area of five rectangular steps, each with width $\Delta t = 2$ s and height equal to the average of the velocities at the beginning and end of each step.

0 s to 2 s	$v_{\text{avg}} = 14 \text{ mph} = 6.26 \text{ m/s}$	area = 12.5 m
2 s to 4 s	$v_{\text{avg}} = 37 \text{ mph} = 16.5 \text{ m/s}$	area = 33.0 m
4 s to 6 s	$v_{\text{avg}} = 53 \text{ mph} = 23.7 \text{ m/s}$	area = 47.4 m
6 s to 8 s	$v_{\text{avg}} = 65 \text{ mph} = 29.1 \text{ m/s}$	area = 58.2 m
8 s to 10 s	$v_{\text{avg}} = 74 \text{ mph} = 33.1 \text{ m/s}$	area = 66.2 m

The total area under the curve is $\approx 217 \text{ m}$, so the distance traveled in 10 s is $\approx 217 \text{ m}$.